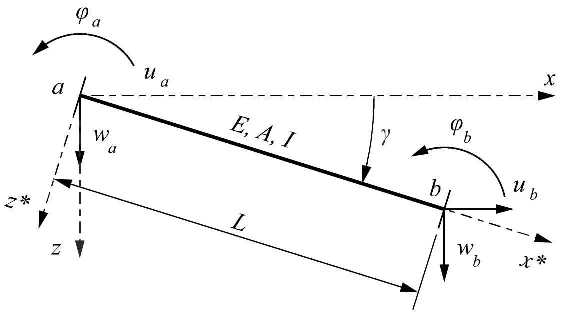
Tabulka 11.4. Globální matice tuhosti prutu konstantního průřezu

(a) Prut oboustranně monoliticky připojený

$c = \cos\gamma$

$s = \sin\gamma$

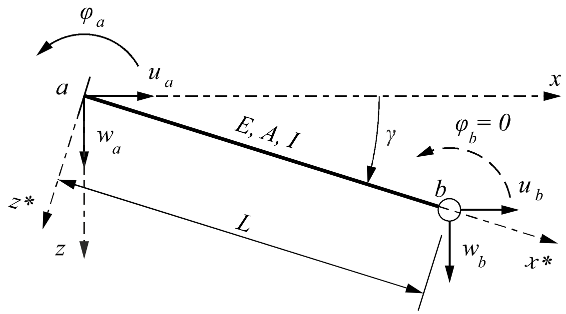


$$k_{ab} = \left[\begin{array}{ccc|ccc}
\frac{EA}{L}c^2+\frac{12EI}{L^3}s^2 & \left(\frac{EA}{L}-\frac{12EI}{L^3}\right)cs & \frac{6EI}{L^2}s & -\left(\frac{EA}{L}c^2+\frac{12EI}{L^3}s^2\right) & -\left(\frac{EA}{L}-\frac{12EI}{L^3}\right)cs & \frac{6EI}{L^2}s \\
\left(\frac{EA}{L}-\frac{12EI}{L^3}\right)cs & \frac{EA}{L}s^2+\frac{12EI}{L^3}c^2 & -\frac{6EI}{L^2}c & -\left(\frac{EA}{L}-\frac{12EI}{L^3}\right)cs & -\left(\frac{EA}{L}s^2+\frac{12EI}{L^3}c^2\right) & -\frac{6EI}{L^2}c \\
\frac{6EI}{L^2}s & -\frac{6EI}{L^2}c & \frac{4EI}{L} & -\frac{6EI}{L^2}s & \frac{6EI}{L^2}c & \frac{2EI}{L} \\
\hline
-\left(\frac{EA}{L}c^2+\frac{12EI}{L^3}s^2\right) & -\left(\frac{EA}{L}-\frac{12EI}{L^3}\right)cs & -\frac{6EI}{L^2}s & \frac{EA}{L}c^2+\frac{12EI}{L^3}s^2 & \left(\frac{EA}{L}-\frac{12EI}{L^3}\right)cs & -\frac{6EI}{L^2}s \\
-\left(\frac{EA}{L}-\frac{12EI}{L^3}\right)cs & -\left(\frac{EA}{L}s^2+\frac{12EI}{L^3}c^2\right) & \frac{6EI}{L^2}c & \left(\frac{EA}{L}-\frac{12EI}{L^3}\right)cs & \frac{EA}{L}s^2+\frac{12EI}{L^3}c^2 & \frac{6EI}{L^2}c \\
\frac{6EI}{L^2}s & -\frac{6EI}{L^2}c & \frac{2EI}{L} & -\frac{6EI}{L^2}s & \frac{6EI}{L^2}c & \frac{4EI}{L}
\end{array}\right]$$

(b) Prut pravostranně kloubově připojený

$c = \cos\gamma$

$s = \sin\gamma$

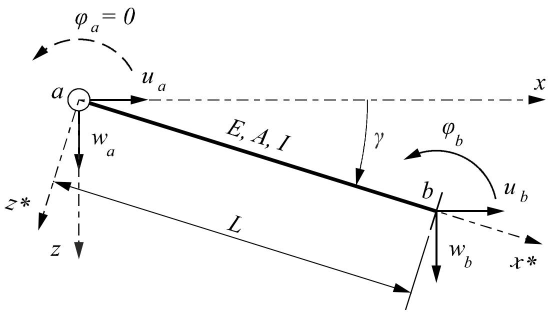


$$k_{ab} = \left[\begin{array}{ccc|ccc}
\frac{EA}{L}c^2+\frac{3EI}{L^3}s^2 & \left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & \frac{3EI}{L^2}s & -\left(\frac{EA}{L}c^2+\frac{3EI}{L^3}s^2\right) & -\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & 0 \\
\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & \frac{EA}{L}s^2+\frac{3EI}{L^3}c^2 & -\frac{3EI}{L^2}c & -\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & -\left(\frac{EA}{L}s^2+\frac{3EI}{L^3}c^2\right) & 0 \\
\frac{3EI}{L^2}s & -\frac{3EI}{L^2}c & \frac{3EI}{L} & -\frac{3EI}{L^2}s & \frac{3EI}{L^2}c & 0 \\
\hline
-\left(\frac{EA}{L}c^2+\frac{3EI}{L^3}s^2\right) & -\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & -\frac{3EI}{L^2}s & \frac{EA}{L}c^2+\frac{3EI}{L^3}s^2 & \left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & 0 \\
-\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & -\left(\frac{EA}{L}s^2+\frac{3EI}{L^3}c^2\right) & \frac{3EI}{L^2}c & \left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & \frac{EA}{L}s^2+\frac{3EI}{L^3}c^2 & 0 \\
0 & 0 & 0 & 0 & 0 & 0
\end{array}\right]$$

(c) Prut levostranně kloubově připojený

$c = \cos\gamma$

$s = \sin\gamma$

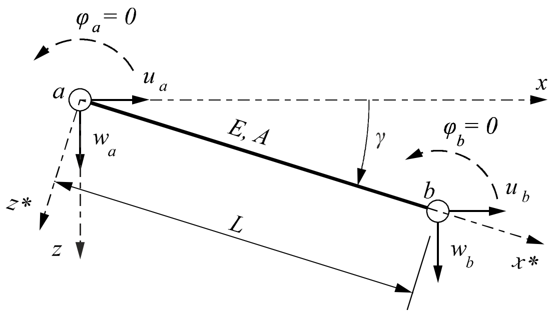


$$k_{ab} = \left[\begin{array}{ccc|ccc}
\frac{EA}{L}c^2+\frac{3EI}{L^3}s^2 & \left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & 0 & -\left(\frac{EA}{L}c^2+\frac{3EI}{L^3}s^2\right) & -\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & \frac{3EI}{L^2}s \\
\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & \frac{EA}{L}s^2+\frac{3EI}{L^3}c^2 & 0 & -\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & -\left(\frac{EA}{L}s^2+\frac{3EI}{L^3}c^2\right) & -\frac{3EI}{L^2}c \\
0 & 0 & 0 & 0 & 0 & 0 \\
\hline
-\left(\frac{EA}{L}c^2+\frac{3EI}{L^3}s^2\right) & -\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & 0 & \frac{EA}{L}c^2+\frac{3EI}{L^3}s^2 & \left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & -\frac{3EI}{L^2}s \\
-\left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & -\left(\frac{EA}{L}s^2+\frac{3EI}{L^3}c^2\right) & 0 & \left(\frac{EA}{L}-\frac{3EI}{L^3}\right)cs & \frac{EA}{L}s^2+\frac{3EI}{L^3}c^2 & \frac{3EI}{L^2}c \\
\frac{3EI}{L^2}s & -\frac{3EI}{L^2}c & 0 & -\frac{3EI}{L^2}s & \frac{3EI}{L^2}c & \frac{3EI}{L}
\end{array}\right]$$

(d) Prut oboustranně kloubově připojený

$c = \cos\gamma$

$s = \sin\gamma$



$$k_{ab} = \frac{EA}{L}\left[\begin{array}{ccc|ccc}
c^2 & cs & 0 & -c^2 & -cs & 0 \\
cs & s^2 & 0 & -cs & -s^2 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
\hline
-c^2 & -cs & 0 & c^2 & cs & 0 \\
-cs & -s^2 & 0 & cs & s^2 & 0 \\
0 & 0 & 0 & 0 & 0 & 0
\end{array}\right]$$

K výpočtu lokálních koncových sil z globálních parametrů deformace:

$$\hat{\boldsymbol{R}}^*_{ab} = \boldsymbol{k}^*_{ab}\boldsymbol{r}^*_{ab} = \boldsymbol{k}^*_{ab}\boldsymbol{T}_{ab}\boldsymbol{r}_{ab} = \frac{EA}{L}\left[\begin{array}{ccc|ccc}
c & s & 0 & -c & -s & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
\hline
-c & -s & 0 & c & s & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0
\end{array}\right]\boldsymbol{r}_{ab}$$