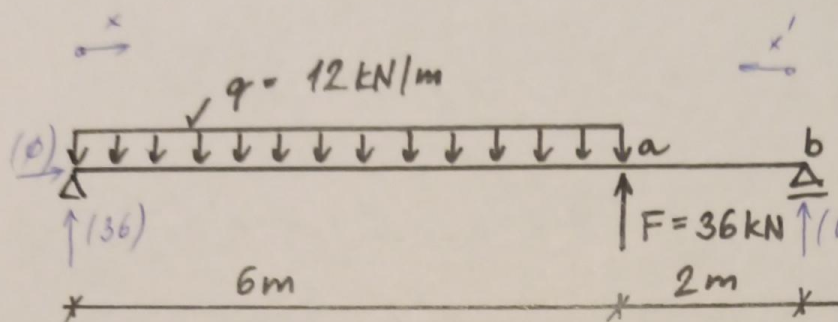
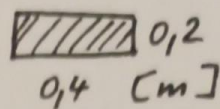
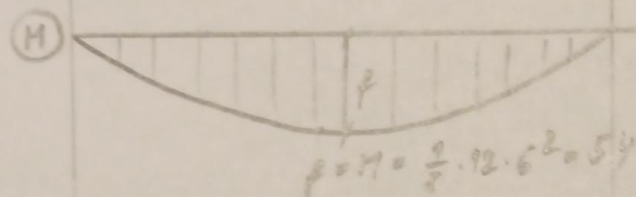


SPočÍTEJTE PRŮHYB V BODĚ „a“ A PootoČENÍ V BODĚ „b“. $E = 240 \text{ GPa}$, PRŮŘEZ

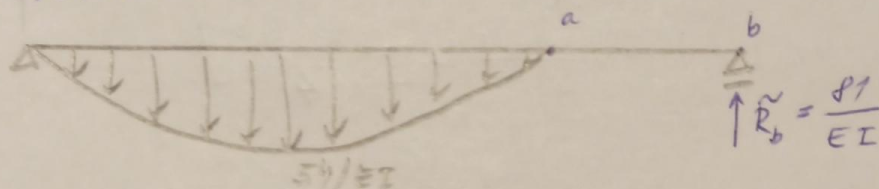


$$EI = 240 \cdot 10^9 \cdot \frac{1}{12} \cdot 0,4 \cdot 0,2^3$$

$$EI = 64000 \text{ kPa} \cdot \text{m}^4$$



MOHRHOVA METODA:
Fiktivní nosník:



$$\underline{w_a = \tilde{M}_a = \tilde{R}_b \cdot 2 = \frac{81}{EI} \cdot 2 = \frac{162}{EI} = \frac{162}{64000} = 2,53125 \cdot 10^{-3} \text{ m}}$$

$$\underline{\varphi_b = \tilde{V}_b = -\tilde{R}_b = -\frac{81}{EI} = -\frac{81}{64000} = -1,265625 \cdot 10^{-3} \text{ rad}}$$

CLEBSCHOVA METODA:

$$M(x) = 36x - 12 \frac{x^2}{2} \Big|_{x \geq 6} + 12 \frac{(x-6)^2}{2} + 36(x-6)$$

$$\varphi(x) = -\frac{1}{EI} \left[C_1 + 36 \frac{x^2}{2} - 6 \frac{x^3}{3} \Big|_{x \geq 6} + 6 \frac{(x-6)^3}{3} + 36 \frac{(x-6)^2}{2} \right]$$

$$w(x) = -\frac{1}{EI} \left[C_2 + C_1 x + 18 \frac{x^3}{3} - 2 \frac{x^4}{4} \Big|_{x \geq 6} + 2 \frac{(x-6)^4}{4} + 18 \frac{(x-6)^3}{3} \right]$$

Ohranové podmínky:

$$w(x=0)=0 \rightarrow \underline{c_2=0}$$

$$w(x=8)=0 \rightarrow 0+8c_1+1080=0 \rightarrow \underline{c_1=-135}$$

$$\underline{w_a = w(x=6) = -\frac{1}{64000} \left[0 - 135 \cdot 6 + 6 \cdot 6^3 - \frac{1}{2} \cdot 6^4 \right] = \frac{162}{64000} = 2,53125 \cdot 10^{-3} \text{ m}}$$

$$\underline{\varphi_b = \varphi(x=8) = -\frac{1}{64000} \left[-135 + 18 \cdot 8^2 - 2 \cdot 8^3 + 2 \cdot 2^3 + 18 \cdot 2^2 \right] = \frac{-81}{64000} = -1,265625 \cdot 10^{-3} \text{ rad}}$$

CLEBSCHOVA METODA PRO x' JDOUCÍ ZPRAVA:

$$M(x') = \left| +36(x'-2) - 12 \frac{(x'-2)^2}{2} \right|_{x' \geq 2}$$

$$\varphi(x') = -\frac{1}{EI} \left[c_1 \left| +36 \frac{(x'-2)^2}{2} - 6 \frac{(x'-2)^3}{3} \right|_{x' \geq 2} \right]$$

$$w(x') = -\frac{1}{EI} \left[c_2 + c_1 x' \left| +18 \frac{(x'-2)^3}{3} - 2 \frac{(x'-2)^4}{4} \right|_{x' \geq 2} \right]$$

Ohranové podmínky:

$$w(x'=0)=0 \rightarrow \underline{c_2=0}$$

$$w(x'=8)=0 \rightarrow 0+8c_1+648=0 \rightarrow \underline{c_1=-81}$$

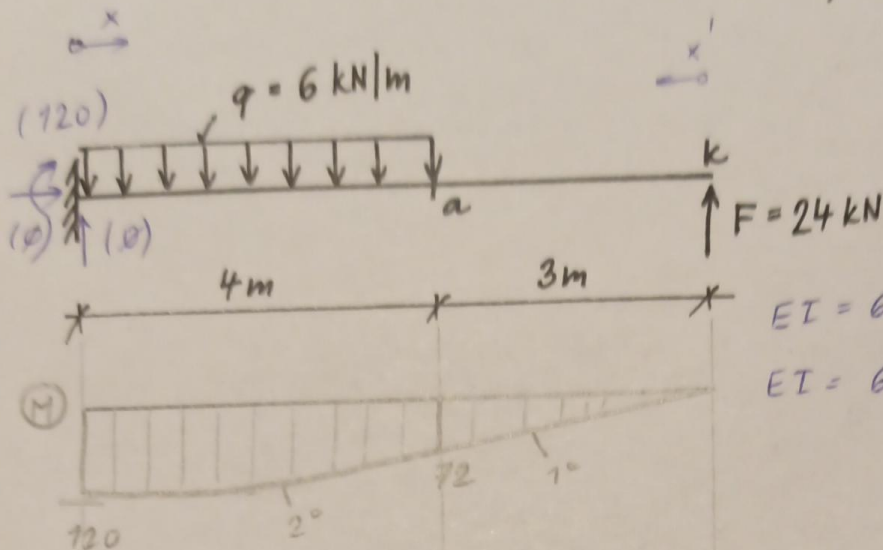
$$\underline{w_a = w(x'=2) = -\frac{1}{64000} \left[0 + (-81) \cdot 2 \right] = \frac{162}{64000} = 2,53125 \cdot 10^{-3} \text{ m}}$$

$$\underline{\varphi_b = \varphi(x'=0) = +\frac{1}{64000} \left[-81 \right] = \frac{-81}{64000} = -1,265625 \cdot 10^{-3} \text{ rad}}$$

OPAČNÉ ZNAMÉNKO PRO VÝPOČET ZPRAVA ($\varphi_L = -\varphi_P$)

SPočíTEJTE PootočENí V BODE, "a" A
PRŮHYB V BODE "k". $E = 60 \text{ GPa}$, PRŮŘEZ

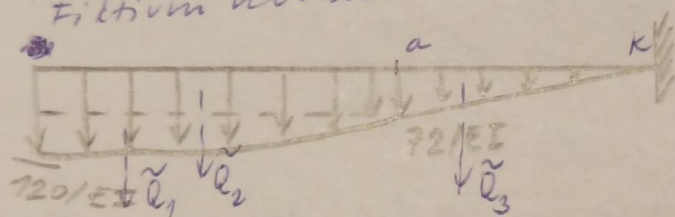
 0,4
0,2 [m]



$$EI = 60 \cdot 10^6 \cdot \frac{1}{2} \cdot 0,2 \cdot 0,4^3$$

$$EI = 64000 \text{ kPa} \cdot \text{m}^4$$

MOHROVA METODA:
Fiktivní nosník:



$$\underline{y_a = \tilde{v}_a = -\tilde{Q}_1 - \tilde{Q}_2 = -\frac{2}{3} \cdot 4 \cdot \frac{48}{EI} - \frac{72}{EI} \cdot 4 = \frac{-416}{EI} = \frac{-416}{64000} = -6,5 \cdot 10^{-3} \text{ m}}$$

$$\underline{w_k = \tilde{m}_k = -\tilde{Q}_1 \cdot (3 + \frac{5}{8} \cdot 4) - \tilde{Q}_2 \cdot 5 - \tilde{Q}_3 \cdot 2 = -\frac{2}{3} \cdot 4 \cdot \frac{48}{EI} \cdot 5,5 - \frac{72}{EI} \cdot 4 \cdot 5 - \frac{1}{2} \cdot 3 \cdot \frac{72}{EI} \cdot 2 = \frac{-2360}{EI} = \frac{-2360}{64000} = -36,875 \cdot 10^{-3} \text{ m}}$$

CLERCHIOVA METODA:

$$M(x) = 120 - 6 \frac{x^2}{2} \Big|_{x \leq 4} + 6 \frac{(x-4)^2}{2} \Big|_{x > 4}$$

$$\varphi(x) = -\frac{1}{EI} \left[C_1 + 120x - 3 \frac{x^3}{3} \Big|_{x \leq 4} + 3 \frac{(x-4)^3}{3} \Big|_{x > 4} \right]$$

$$w(x) = -\frac{1}{EI} \left[C_2 + C_1 x + 120 \frac{x^2}{2} - \frac{x^4}{4} \Big|_{x \leq 4} + \frac{(x-4)^4}{4} \Big|_{x > 4} \right]$$

Ohraničovací podmínky:

$$w(x=0)=0 \rightarrow C_2=0$$

$$\varphi(x=0)=0 \rightarrow \underline{C_1=0}$$

$$\underline{\varphi_a = \varphi(x=4)} = -\frac{1}{64000} [0 + 120 \cdot 4 - 4^3] = \frac{-416}{64000} = \underline{-6,5 \cdot 10^{-3} \text{ m}}$$

$$\underline{w_k = w(x=7)} = -\frac{1}{64000} [0 + 10 \cdot 7 + 60 \cdot 7^2 - \frac{7^4}{4} + \frac{3^4}{4}] = \frac{-2360}{64000} =$$
$$= \underline{-36,875 \cdot 10^{-3} \text{ m}}$$

CLEBBOCHOVA METODA PRO x' JDOUCÍ ZPRAVA:

$$M(x') = 24 \cdot x' \Big|_{x'>3} - 6 \frac{(x'-3)^2}{2}$$

$$\varphi(x') = -\frac{1}{EI} \left[\overset{C_1 + C_2}{\cancel{12}} \frac{x'^2}{2} \Big|_{x'>3} - 3 \frac{(x'-3)^3}{3} \right]$$

$$w(x') = -\frac{1}{EI} \left[\overset{C_2 + C_1 x'}{\cancel{12}} \frac{x'^3}{3} \Big|_{x'>3} - \frac{(x'-3)^4}{4} \right]$$

Ohraničovací podmínky:

$$w(x'=7)=0 \rightarrow C_2 + C_1 \cdot 7 + 1308 = 0$$

$$\varphi(x'=7)=0 \rightarrow C_1 + 524 = 0 \rightarrow \underline{C_1 = -524}$$

$$\underline{C_2 = 2360}$$

$$\underline{\varphi_a = -\varphi(x'=3)} = +\frac{1}{64000} [-524 + 12 \cdot 3^2] = \frac{-416}{64000} = \underline{-6,5 \cdot 10^{-3} \text{ m}}$$

OPRAVNĚNÉ ZNAMÉNKO PŘI ŘEŠENÍ ZPRAVA ($\varphi_L = -\varphi_R$)

$$\underline{w_k = w(x'=0)} = -\frac{1}{64000} [2360] = \frac{-2360}{64000} = \underline{-36,875 \cdot 10^{-3} \text{ m}}$$