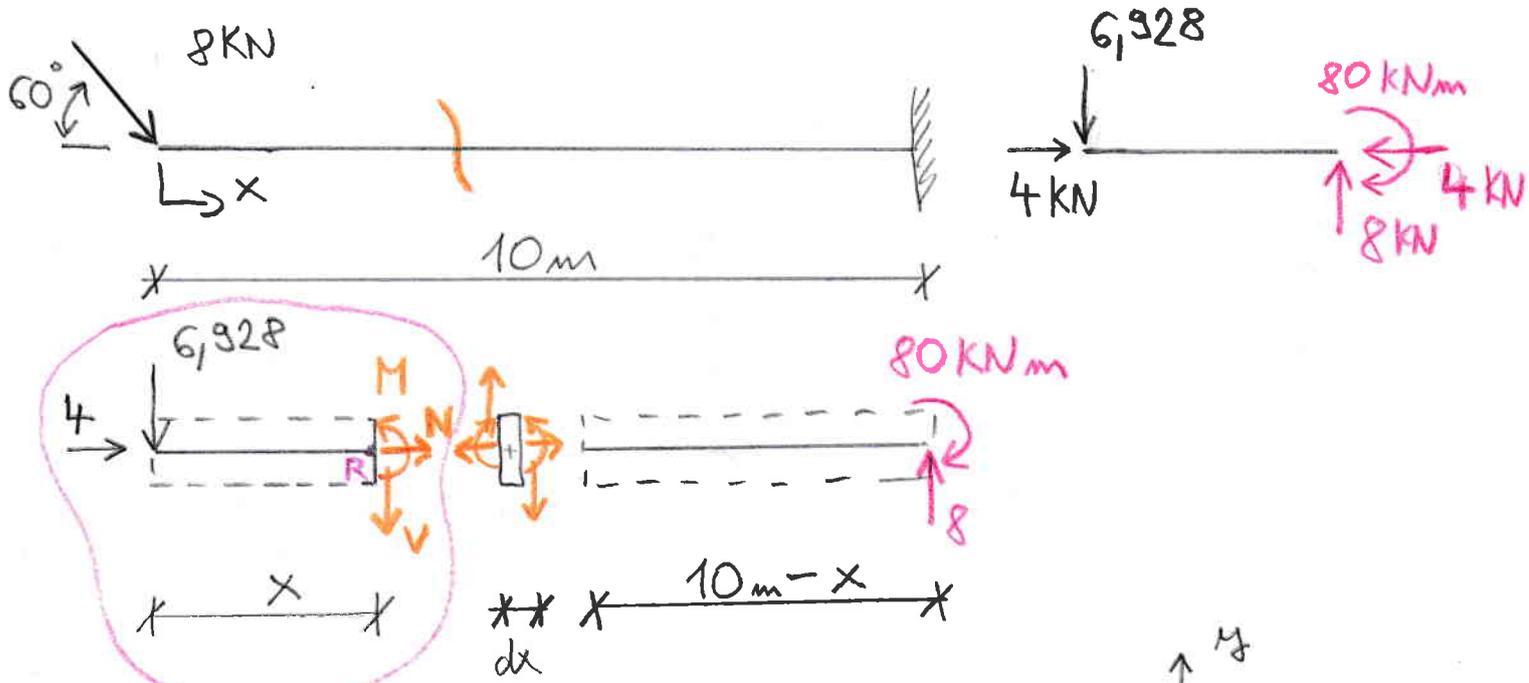


# ZÁKLADY STAVEBNÍ MECHANIKY

BDA001

Rovinné přímé nosníky zatížené libovolným rovnoměrným zatížením, výpočet reakcí ve vazbách, výpočet a vykreslení diagramů vnitřních sil.

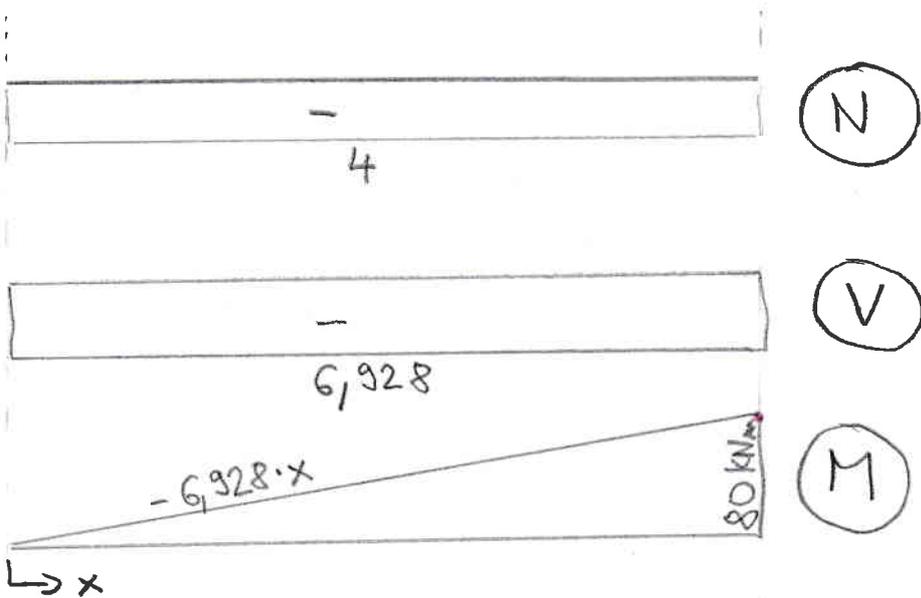
Zdeněk Kala

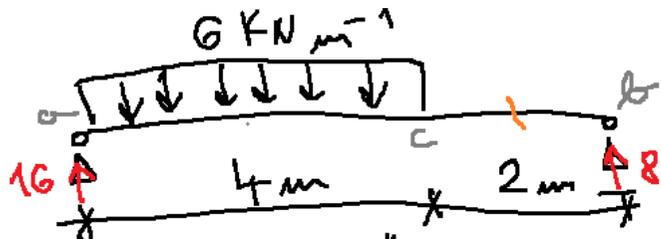


ROVNOVAHA

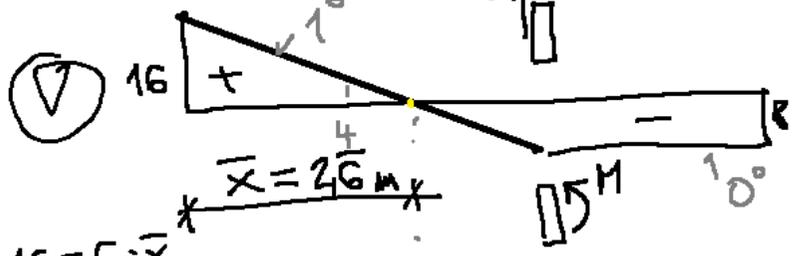
$$\begin{aligned} \sum F_x = 0 & \quad 4 + N = 0 \Rightarrow N = -4 \\ \sum F_y = 0 & \quad -6,928 - V = 0 \Rightarrow V = -6,928 \\ \sum M_R = 0 & \quad 6,928 \cdot x + M = 0 \Rightarrow M = -6,928 \cdot x \end{aligned}$$

$$V = \frac{dM}{dx}$$



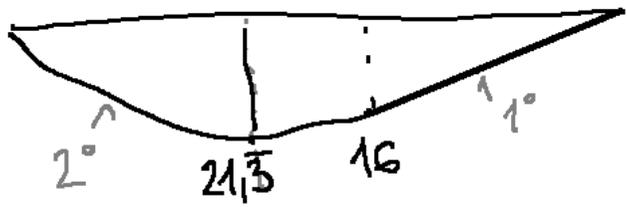


Ⓢ

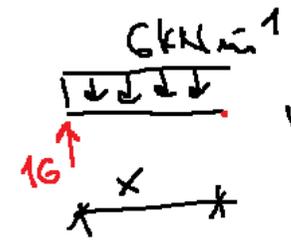


$16 = 6 \cdot \bar{x}$

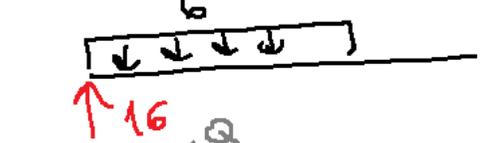
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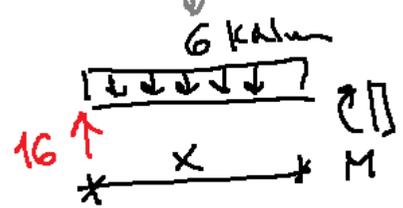
$\sum M_a = 0 \quad -24 \cdot 2 + R_b \cdot 6 = 0$   
 $R_b = 8 \text{ kN}$   
 $\sum M_b = 0 \quad 24 \cdot 4 - R_a \cdot 6 = 0$   
 $R_a = 16 \text{ kN}$



$V(x) = 16 - 6 \cdot x \quad x \in \langle 0; 4 \text{ m} \rangle$

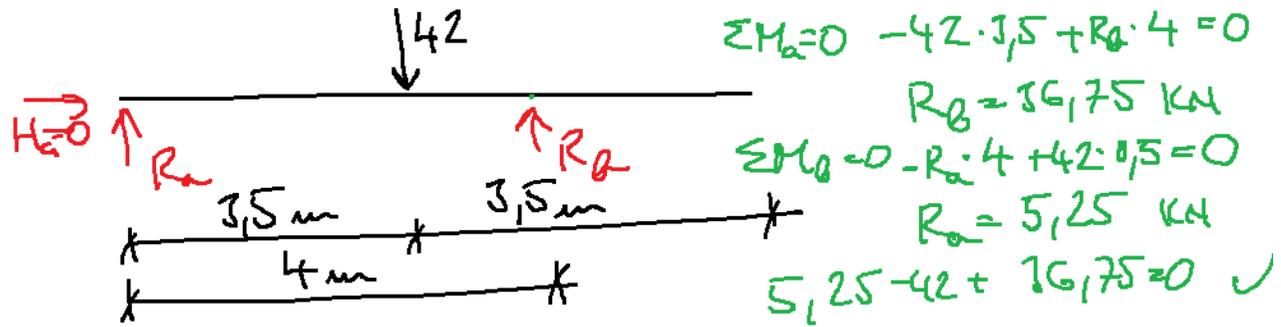
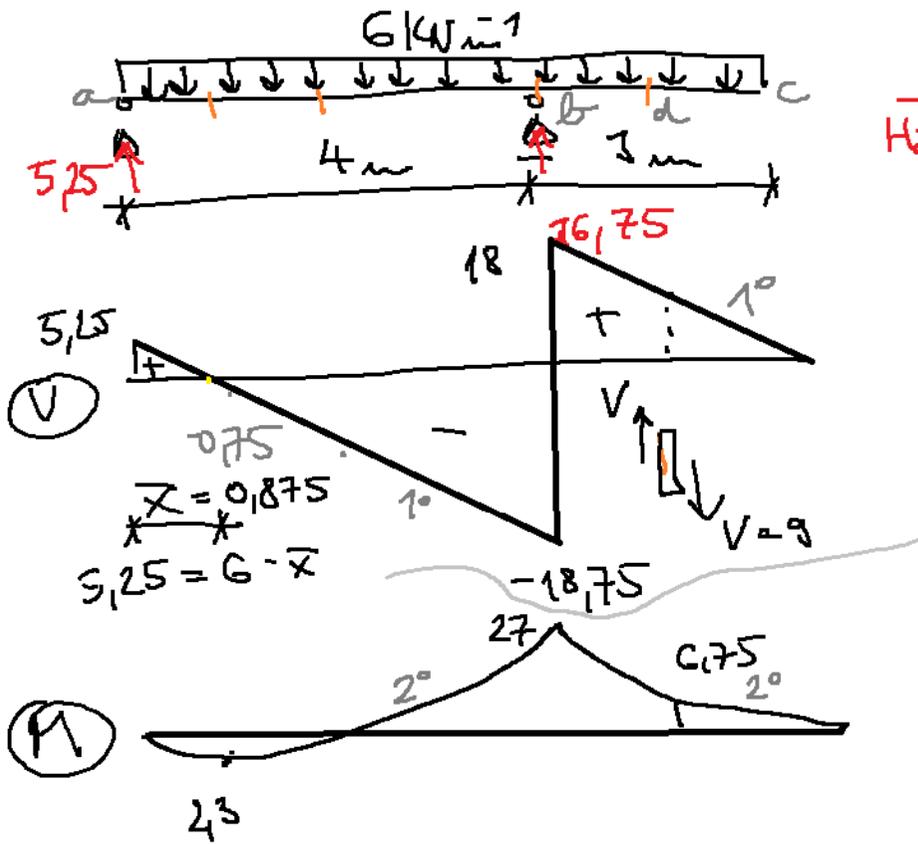


$V(x) = 16 - 6 \cdot 4 \quad x \in \langle 4; 6 \text{ m} \rangle$   
 $= -8 \text{ kN}$



$M(x) = 16 \cdot x - 6 \cdot x \cdot \frac{x}{2} = 16 \cdot x - 3x^2$   
 $\max M = 16 \cdot 2\sqrt{6} - 3 \cdot (2\sqrt{6})^2 = 21,3 \text{ kNm}$

$V(x) = \frac{dM}{dx} = \frac{d(16 \cdot x - 3x^2)}{dx} = 16 - 6 \cdot x$



$$\sum M_b = 0 \quad -42 \cdot 3,5 + R_a \cdot 4 = 0$$

$$R_a = 36,75 \text{ kN}$$

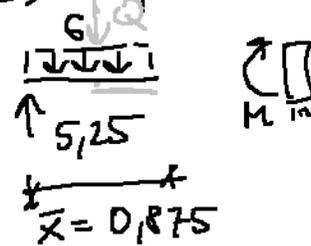
$$\sum M_a = 0 \quad -R_b \cdot 4 + 42 \cdot 0,5 = 0$$

$$R_b = 5,25 \text{ kN}$$

$$5,25 - 42 + 36,75 = 0 \quad \checkmark$$

$$M_a = 0$$

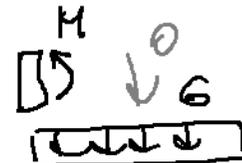
$$M(0,875) = 5,25 \cdot 0,875 - 6 \cdot x \cdot \frac{x}{2} = 2,3 \text{ kNm}$$

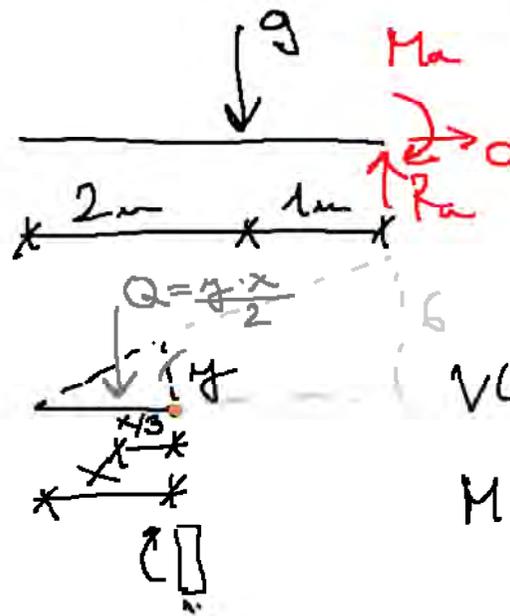
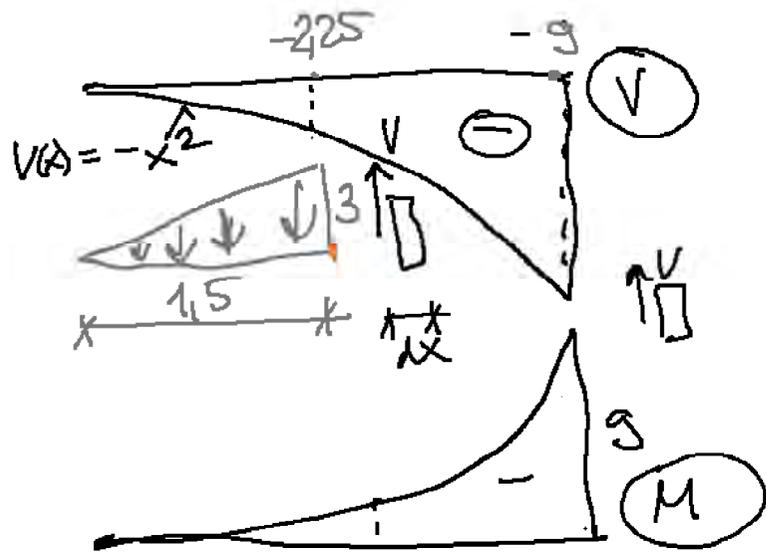
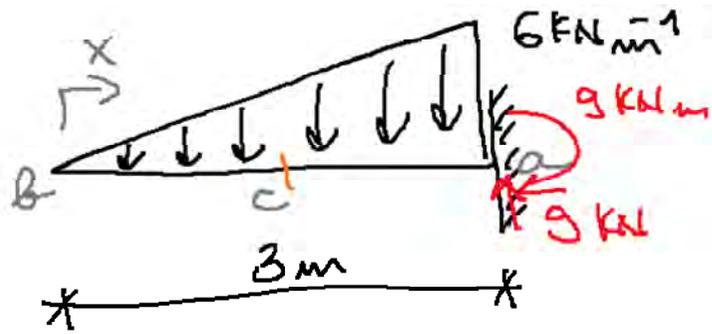


$Q$  [kN]  
 $M$  [kNm]

$$M_d = -6 \cdot 1,5 \cdot \frac{1,5}{2} = -6,75 \text{ kNm}$$

$$M_b = -6 \cdot 3 \cdot 1,5 = -27 \text{ kNm}$$





$$\sum F_y = 0 \quad -9 + R_a = 0 \quad R_a = 9 \text{ kN}$$

$$\sum M_a = 0 \quad 9 \cdot 1 - M_a = 0 \quad M_a = 9 \text{ kNm}$$

$$\frac{6}{3} = \frac{y}{x} \Rightarrow y = 2 \cdot x$$

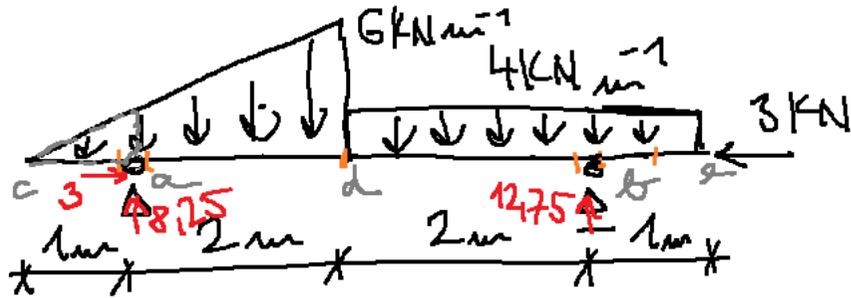
$$V(x) = Q = \frac{y \cdot x}{2} = \frac{2 \cdot x \cdot x}{2} = -x^2$$

$$M(x) = -Q \cdot \frac{x}{3} = -\frac{y \cdot x}{2} \cdot \frac{x}{3} =$$

$$= -\frac{2 \cdot x \cdot x}{2} \cdot \frac{x}{3} = -\frac{x^3}{3}$$

$$V = \frac{dM}{dx} = \frac{d(-x^3/3)}{dx} = -x^2$$

$$\max M = -\frac{3^3}{3} = -9 \text{ kNm}$$



$$\sum M_a = 0 \quad -9 \cdot 1 - 12 \cdot 3,5 + R_b \cdot 4 = 0$$

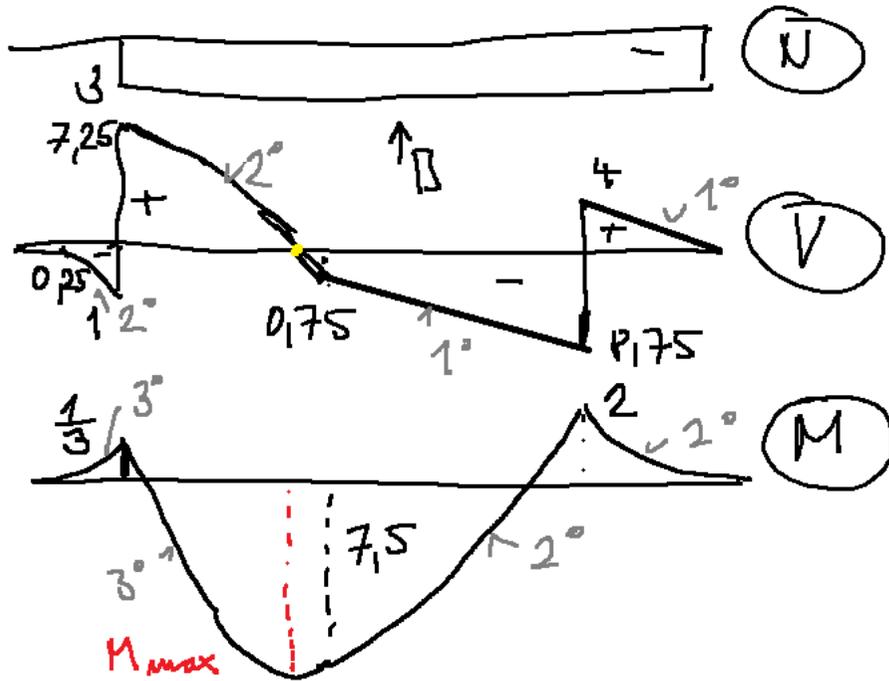
$$R_b = 12,75 \text{ kN}$$

$$\sum M_b = 0 \quad -R_a \cdot 4 + 9 \cdot 3 + 12 \cdot 0,5 = 0$$

$$R_a = 8,25 \text{ kN}$$

$$\sum F_y = 0 \quad 8,25 - 9 - 12 + 12,75 = 0$$

$$\sum F_x = 0 \quad H_a - 3 = 0 \quad H_a = 3 \checkmark$$



$$L V_a = -\frac{2 \cdot 1}{2} = -1 \text{ kN}$$

$$R V_a = L V_a + R,25 = 7,25$$

$$V_d = 8,25 - 9 = -0,75$$

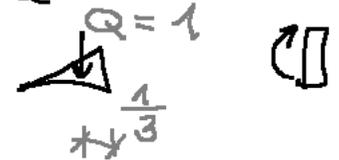
$$R V_b = 4 \cdot 1 = 4$$

$$L V = 4 \cdot 1 - 12,75 = -8,75$$

$$-0,75 - 4 \cdot 2 = -8,75$$

$$V_d - 4 \cdot 2 = -8,75$$

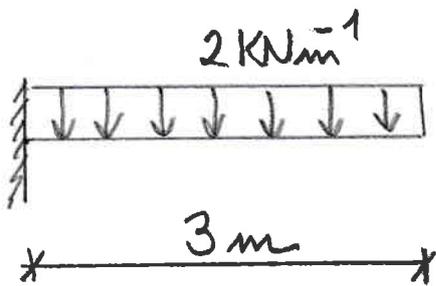
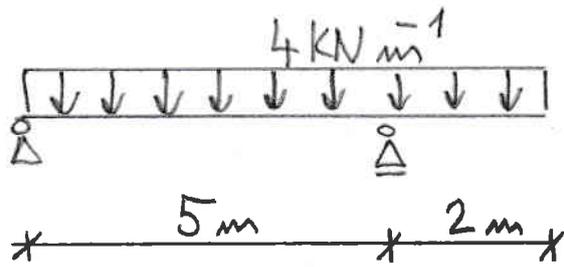
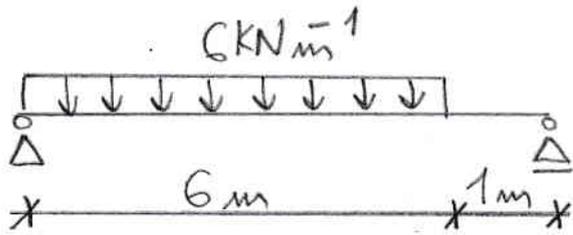
$$M_a = -1 \cdot \frac{1}{3} = -\frac{1}{3}$$



$$M_b = 4 \cdot 1 \cdot 0,5 = 2 \text{ kNm}$$

$$\int 5 - 2$$

$$M_d = 8,25 \cdot 2 - 9 \cdot 1 = 7,5 \text{ kNm}$$



VLOŽIT DO TEAMS  
DO 13.3. VEČER