HOW TO DESIGN AND CHECK SIMPLE JOINTS?

...worked examples for NOA019

SECONDARY BEAM TO PRIMARY BEAM CONNECTION



PRIMARY BEAM TO COLUMN CONNECTION



BRACING CONNECTIONS



WORKED EXAMPLE 1:

BRACING CONNECTION IN ALTERNATIVE 1



Normal force in bracing diagonal

Due to wind load (design of vertical bracing, only tension diagonal is active)

 $N_{\rm Ed} = 454$ kN

Diagonal section: $2 \times L80/8$, thickness of leg $t_a = 8$ mm, steel S235

Gusset plate: thickness $t_p = 15$ mm, steel S235

Bolts

Design: bolts M20, material 8.8

$f_{\rm yb} = 640 \text{ MPa}$	bolt yield strength
$f_{\rm ub} = 800 \text{ MPa}$	bolt ultimate strength
d = 20 mm	bolt diameter
$d_0 = 22 \text{ mm}$	bolt hole diameter
A = 314 mm	gross cross section of the bolt
$A_{\rm s} = 245 {\rm mm}$	tensile stress area of the bolt
$e_1 = 50 \text{ mm}$	end distance
$p_1 = 80 \text{ mm}$	spacing
$e_2 = 35 \text{ mm}$	edge distance (smaller of them



=> bolt connection in shear

Shear resistance

$$F_{\rm v,Rd} = n_{\rm s} \cdot \frac{\alpha_{\rm v} \cdot f_{\rm ub} \cdot A_{\rm s}}{\gamma_{\rm M2}} = 2 \cdot \frac{0.6 \cdot 800 \cdot 245}{1.25} = 188 \text{ kN}$$

where

 $n_{\rm s}$ is number of shear planes

 α_v is factor for 8.8 if shear plane passes through the threated portion of the bolt

 $A_{\rm s}$ is used if shear planes passes through threated portion of the bolt

Bearing resistance

$$F_{\rm b,Rd} = \frac{k_1 \cdot \alpha_{\rm b} \cdot f_{\rm u} \cdot d \cdot t}{\gamma_{\rm M2}} = \frac{2.5 \cdot 0.76 \cdot 360 \cdot 20 \cdot 15}{1.25} = 164 \text{ kN}$$

where

$$k_{1} = \min\left\{2,8 \cdot \frac{e_{2}}{d_{0}} - 1,7 ; 1,4 \cdot \frac{p_{2}}{d_{0}} - 1,7 ; 2,5\right\} = \min\left\{2,8 \cdot \frac{35}{22} - 1,7 ; -; 2,5\right\} = \min\left\{2,75 ; -; 2,5\right\} = 2,5$$

$$\alpha_{b} = \min\left\{\frac{e_{1}}{3d_{0}}; \frac{p_{1}}{3d_{0}} - \frac{1}{4}; \frac{f_{ub}}{f_{u}}; 1\right\} = \min\left\{\frac{50}{3 \cdot 22}; \frac{80}{3 \cdot 22} - \frac{1}{4}; \frac{800}{360}; 1\right\} = \min\left\{0,76 ; 0,96 ; 2,22 ; 1\right\} = 0,76$$

$$t = \min\left\{t_{p}; 2 \cdot t_{a}\right\} = \min\left\{15; 2 \cdot 8\right\} = 15 \text{ mm}$$

Number of bolts to satisfied condition

$$n_{\text{bolt}} = \frac{N_{\text{Ed}}}{\min\{F_{\text{v,Rd}}; F_{\text{b,Rd}}\}} = \frac{454}{\min\{188; 164\}} = 2,77 \qquad => 3 \text{ bolts M20, 8.8}$$

Angle

Ultimate resistance of the net-cross section at holes

Due to holes for bolts, angle gross cross section is reduced, net area resistance is:

$$N_{u,Rd} = \frac{\beta \cdot A_{net} \cdot f_{u}}{\gamma_{M2}} = \frac{0.59 \cdot 2108 \cdot 360}{1.25} = 358 \text{ kN}$$

where A_{net} is net area of angle without holes for bolts

$$A_{\text{net}} = 2 \cdot (A - d_0 \cdot t_a) = 2 \cdot (1230 - 22 \cdot 8) = 2108 \text{ mm}^2$$

 β is reduction factor for angle connected by one leg according to the table below (linear interpolation for intermediate values of p_1)



Ing. Ondřej PEŠEK, Ph.D.

 $A_{\rm nt}$

 $A_{\rm nv}$

 $N_{\rm Ed}$

Brno University of Technology --- Faculty of Civil Engineering --- Institute of Metal and Timber Structures

Spacing p_1	\leq 2.5 d_0	$\geq 5 d_0$
β_2 for two bolts	0.4	0.7
β_3 for three or more bolts	0.5	0.7

Reliability condition:

$$\frac{N_{\rm Ed}}{N_{\rm u,Rd}} = \frac{454}{358} = 1,27 \ge 1,0 \qquad => condition is not satisfied$$

Block tearing

Due to hole group, diagonal gross cross section is reduced. Design block tearing resistance for bolt group subject to eccentric loading

$$V_{\text{eff,2, Rd}} = \frac{0.5 \cdot f_{\text{u}} \cdot A_{\text{nt}}}{\gamma_{\text{M2}}} + \frac{f_{\text{y}} / \sqrt{3} \cdot A_{\text{nv}}}{\gamma_{\text{M0}}} = \frac{0.5 \cdot 360 \cdot 384}{1.25} + \frac{235 / \sqrt{3} \cdot 2480}{1.00} = 55 + 336 = 391 \,\text{kN}$$

where

 $A_{\rm nt}$ is net area subjected to tension

$$A_{\rm nt} = 2 \cdot t_{\rm a} \cdot (l_{\rm nt}) = 2 \cdot 8 \cdot (35 - 11) = 384 \,{\rm mm}^2$$

 A_{nv} is net area subjected to shear

$$A_{\rm nv} = 2 \cdot t_{\rm a} \cdot (l_{\rm nv}) = 2 \cdot 8 \cdot (50 + 80 + 80 - 22 - 22 - 11) = 2480 \,\rm mm^2$$

$$\frac{N_{\rm Ed}}{V_{\rm eff,2, Rd}} = \frac{454}{391} = 1.16 \ge 1.0 \qquad => condition is not satisfied$$

Gusset plate

Block tearing

Due to hole group, gusset plate gross cross section is reduced. Design block tearing resistance for bolt group subject to eccentric loading



Reliability condition:

$$\frac{N_{\rm Ed}}{V_{\rm eff,2, \, Rd}} = \frac{454}{388} = 1,17 \ge 1,0$$

=> condition is not satisfied

Fillet weld



a = 5 mm	effective throat thickness	of a	fillet	weld
-----------	----------------------------	------	--------	------

- L = 419 mm effective length of a fillet weld
- e = 68 mm force eccentricity (brace diagonal axis) to centroid of the fillet weld

$$\tau_{\rm II} = \frac{N_{\rm h,Ed}}{2 \cdot L \cdot a} = \frac{389.10^3}{2 \cdot 419 \cdot 5} = 93 \text{ MPa}$$

$$\sigma_{\rm v} = \frac{N_{\rm v,Ed}}{2 \cdot L \cdot a} = \frac{233.10^3}{2 \cdot 419 \cdot 5} = 56 \text{ MPa}$$

$$\sigma_{\rm M} = \frac{N_{\rm v,Ed} \cdot e}{2 \cdot \frac{1}{6} \cdot L^2 \cdot a} = \frac{233.10^3 \cdot 68}{2 \cdot \frac{1}{6} \cdot 419^2 \cdot 5} = 54 \text{ MPa}$$

$$\sigma_{\perp} = \tau_{\perp} = \frac{\sigma_{\rm v} + \sigma_{\rm M}}{\sqrt{2}} = \frac{56 + 54}{\sqrt{2}} = 78 \text{ MPa}$$

Reliability conditions:

 $\sqrt{\sigma_{\perp}^{2} + 3 \cdot (\tau_{\perp}^{2} + \tau_{\Pi}^{2})} \leq \frac{f_{u}}{\beta_{w} \cdot \gamma_{M2}}$ $\sqrt{78^{2} + 3 \cdot (78^{2} + 93^{2})} \leq \frac{360}{0.8 \cdot 1.25}$ $224 \text{ MPa} \leq 360 \text{ MPa} \qquad => \text{ condition is satisfied}$ $\sigma_{\perp} \leq \frac{0.9 \cdot f_{u}}{\gamma_{M2}}$

78 MPa
$$\leq \frac{0.9 \cdot 360}{1.25} = 259$$
 MPa $=>$ condition is satisfied

where β_{w} is correlation factor according to the table 1.

Table 1.

Steel grade	$eta_{ m w}$
S235	0.80
S275	0.85
\$355	0.90
S420	1.00
S460	1.00

WORKED EXAMPLE 2:



Force in connection

Action on connection is reaction of secondary beam

 $F_{\rm Ed} = 70 \, \rm kN$

Secondary beam: IPE 200, thickness of web $t_w = 5,6$ mm, steel S235

Fin plate: thickness $t_p = 10$ mm, steel S235

Bolts

Design: bolts M16, material 8.8

$f_{\rm yb} = 640 \ {\rm MPa}$	bolt yield strength	
$f_{\rm ub} = 800 \text{ MPa}$	bolt ultimate strength	
d = 16 mm	bolt diameter	
$d_0 = 18 \text{ mm}$	bolt hole diameter	
A = 201 mm	gross cross section of the bolt	
$A_{\rm s} = 157 \text{ mm}$	tensile stress area of the bolt	
$e_1 = 40 \text{ mm}$	end distance	
$p_1 = 60 \text{ mm}$	spacing	
$e_2 = 35 \text{ mm}$	edge distance (smaller of them	
=> bolt connection in shear		



Shear force per one bolt

$$F_{\rm v,Ed} = \frac{F_{\rm Ed}}{n_{\rm bolt}} = \frac{70}{2} = 35 \,\rm kN$$

Shear resistance

Shear resistance per one bolt

$$F_{\rm v,Rd} = n_{\rm s} \cdot \frac{\alpha_{\rm v} \cdot f_{\rm ub} \cdot A_{\rm s}}{\gamma_{\rm M2}} = 1 \cdot \frac{0.6 \cdot 800 \cdot 157}{1.25} = 60 \text{ kN}$$

where

 $n_{\rm s}$ is number of shear planes

- α_v is factor for 8.8 if shear plane passes through the threated portion of the bolt
- $A_{\rm s}$ is used if shear planes pass through threated portion of the bolt

Reliability criterion

$$\frac{F_{\rm v,Ed}}{F_{\rm v,Rd}} = \frac{35}{60} = 0,58 \le 1,0 \qquad => condition is satisfied$$

Bearing resistance

Bearing resistance per one bolt

$$F_{\rm b,Rd} = \frac{k_1 \cdot \alpha_{\rm b} \cdot f_{\rm u} \cdot d \cdot t}{\gamma_{\rm M2}} = \frac{2,5 \cdot 0,74 \cdot 360 \cdot 16 \cdot 5,6}{1,25} = 48 \text{ kN}$$

where

$$k_{1} = \min\left\{2,8 \cdot \frac{e_{2}}{d_{0}} - 1,7 ; 1,4 \cdot \frac{p_{2}}{d_{0}} - 1,7 ; 2,5\right\} = \min\left\{2,8 \cdot \frac{35}{18} - 1,7 ; -; 2,5\right\} = \min\left\{3,74 ; -; 2,5\right\} = 2,5$$

$$\alpha_{b} = \min\left\{\frac{e_{1}}{3d_{0}} ; \frac{p_{1}}{3d_{0}} - \frac{1}{4} ; \frac{f_{ub}}{f_{u}} ; 1\right\} = \min\left\{\frac{40}{3 \cdot 18} ; \frac{60}{3 \cdot 18} - \frac{1}{4} ; \frac{800}{360} ; 1\right\} = \min\left\{0,74 ; 0,86 ; 2,22 ; 1\right\} = 0,74$$

$$t = \min\left\{t_{p} ; t_{w}\right\} = \min\left\{10 ; 5,6\right\} = 5,6 \text{ nm}$$

Reliability criterion

$$\frac{F_{\rm v,Ed}}{F_{\rm b,Rd}} = \frac{35}{48} = 0,73 \le 1,0 \qquad => condition is satisfied$$

<u>Fin plate</u>

Shear resistance

$$V_{\rm pl,Rd} = \frac{A_{\rm v} \cdot f_{\rm y} / \sqrt{3}}{\gamma_{\rm M0}} = \frac{1400 \cdot 235 / \sqrt{3}}{1,00} = 190 \,\rm kN$$

where A_v is gross cross area of fin plate

$$A_{\rm v} = h_{\rm g} \cdot t_{\rm g} = 140 \cdot 10 = 1400 \,{\rm mm}^2$$

Reliability criterion

$$\frac{F_{\rm Ed}}{V_{\rm pl,Rd}} = \frac{70}{190} = 0.37 \le 1.0 \qquad => condition is satisfied.$$

Block tearing

Due to hole group, fin plate gross cross section is reduced. Design block tearing resistance for bolt group subject to eccentric loading

$$V_{\text{eff,2, Rd}} = \frac{0.5 \cdot f_{\text{u}} \cdot A_{\text{nt}}}{\gamma_{\text{M2}}} + \frac{f_{\text{y}} / \sqrt{3} \cdot A_{\text{nv}}}{\gamma_{\text{M0}}} = \frac{0.5 \cdot 360 \cdot 261}{1.25} + \frac{235 / \sqrt{3} \cdot 730}{1.00} = 38 + 99 = 137 \text{ kN}$$

where

 $A_{\rm nt}$ is net area subjected to tension

$$A_{\rm nt} = t_{\rm p} \cdot (l_{\rm nt}) = 10 \cdot (35 - 9) = 261 \,{\rm mm}^2$$

 $A_{\rm nv}$ is net area subjected to shear

$$A_{\rm nv} = t_{\rm p} \cdot (l_{\rm nv}) = 10 \cdot (60 + 40 - 18 - 9) = 730 \,{\rm mm}^2$$

Reliability condition:

$$\frac{F_{\rm Ed}}{V_{\rm eff,2, Rd}} = \frac{70}{137} = 0.51 \le 1.0 \qquad => condition i$$

Secondary beam

Block tearing

Due to hole group, secondary beam web gross cross section is reduced. Design block tearing resistance for bolt group subject to eccentric loading

$$V_{\text{eff,2, Rd}} = \frac{0.5 \cdot f_{\text{u}} \cdot A_{\text{nt}}}{\gamma_{\text{M2}}} + \frac{f_{\text{y}} / \sqrt{3} \cdot A_{\text{nv}}}{\gamma_{\text{M0}}} = \frac{0.5 \cdot 360 \cdot 146}{1.25} + \frac{235 / \sqrt{3} \cdot 409}{1.00} = 21 + 55 = 76 \text{ kN}$$

where







142 MPa $\leq \frac{0.9 \cdot 360}{1.25} = 259$ MPa => condition is satisfied

WORKED EXAMPLE 3:

PRIMARY BEAM TO COLUMN CONNECTION IN ALTERNATIVE 1



Forces in connection

Action on connection is reaction of primary beam

 $F_{\rm Ed} = 150 \text{ kN}$

Primary beam: castellated beam made of IPE 300, thickness of web $t_w = 7,1$ mm, steel S235

Column: HEB 300, thickness of flange $t_f = 19$ mm, steel S235

End plate: thickness $t_p = 15$ mm, steel S235

Bolts

Design: bolts M16, material 8.8

$f_{\rm yb} = 640 \ { m MPa}$	bolt yield strength
$f_{\rm ub} = 800 \text{ MPa}$	bolt ultimate strength
d = 16 mm	bolt diameter
$d_0 = 18 \text{ mm}$	bolt hole diameter
A = 201 mm	gross cross section of the bolt
$A_{\rm s} = 157 {\rm mm}$	tensile stress area of the bolt
$e_1 = 45 \text{ mm}$	end distance
$p_1 = 95 \text{ mm}$	spacing
$e_2 = 50 \text{ mm}$	edge distance (smaller of them)



 $p_2 = 110 \text{ mm}$ spacing

=> bolt connection in shear

Shear force per one bolt

$$F_{\rm v,Ed} = \frac{F_{\rm Ed}}{n_{\rm bolt}} = \frac{150}{6} = 25 \text{ kN}$$

Shear resistance

Shear resistance per one bolt

$$F_{v,Rd} = n_{s} \cdot \frac{\alpha_{v} \cdot f_{ub} \cdot A_{s}}{\gamma_{M2}} = 1 \cdot \frac{0.6 \cdot 800 \cdot 157}{1.25} = 60 \text{ kN}$$

where

 $n_{\rm s}$ is number of shear planes

 α_v is factor for 8.8 if shear plane passes through the threated portion of the bolt

 $A_{\rm s}$ is used if shear planes pass through threated portion of the bolt

Reliability criterion

$$\frac{F_{\rm v,Ed}}{F_{\rm v,Rd}} = \frac{25}{60} = 0,42 \le 1,0 \qquad => condition is satisfied$$

Bearing resistance

Bearing resistance per one bolt

$$F_{\rm b,Rd} = \frac{k_1 \cdot \alpha_{\rm b} \cdot f_{\rm u} \cdot d \cdot t}{\gamma_{\rm M2}} = \frac{2,5 \cdot 0,83 \cdot 360 \cdot 16 \cdot 15}{1,25} = 143 \,\rm kN$$

where

$$k_{1} = \min\left\{2,8 \cdot \frac{e_{2}}{d_{0}} - 1,7 ; 1,4 \cdot \frac{p_{2}}{d_{0}} - 1,7 ; 2,5\right\} = \min\left\{2,8 \cdot \frac{50}{18} - 1,7 ; 1,4 \cdot \frac{110}{18} - 1,7 ; 2,5\right\} = \min\left\{6,08 ; 6,86 ; 2,5\right\} = 2,5$$

$$\alpha_{b} = \min\left\{\frac{e_{1}}{3d_{0}} ; \frac{p_{1}}{3d_{0}} - \frac{1}{4} ; \frac{f_{ub}}{f_{u}} ; 1\right\} = \min\left\{\frac{45}{3 \cdot 18} ; \frac{95}{3 \cdot 18} - \frac{1}{4} ; \frac{800}{360} ; 1\right\} = \min\left\{0,83 ; 1,51 ; 2,22 ; 1\right\} = 0,83$$

$$t = \min \{t_{p}; t_{f}\} = \min \{15; 19\} = 15 \text{ mm}$$

Reliability criterion

$$\frac{F_{\rm v,Ed}}{F_{\rm b,Rd}} = \frac{25}{143} = 0,17 \le 1,0 \qquad => condition is satisfied$$

End plate

Shear resistance

$$V_{\rm pl,Rd} = \frac{A_{\rm v} \cdot f_{\rm y} / \sqrt{3}}{\gamma_{\rm M0}} = \frac{8400 \cdot 235 / \sqrt{3}}{1,00} = 1140 \,\rm kN$$

where A_v is gross cross area of fin plate

$$A_{\rm v} = 2 \cdot h_{\rm p} \cdot t_{\rm p} = 2 \cdot 280 \cdot 15 = 8400 \,{\rm mm}^2$$

Reliability criterion

$$\frac{F_{\rm Ed}}{V_{\rm pl,Rd}} = \frac{150}{1140} = 0,13 \le 1,0$$



Block tearing

Due to hole group, fin plate gross cross section is reduced. Design block tearing resistance for bolt group subject to concentric loading

=> condition is satisfied

$$V_{\text{eff,1, Rd}} = \frac{f_{\text{u}} \cdot A_{\text{nt}}}{\gamma_{\text{M2}}} + \frac{f_{\text{y}} / \sqrt{3} \cdot A_{\text{nv}}}{\gamma_{\text{M0}}} = \frac{360 \cdot 1230}{1,25} + \frac{235 / \sqrt{3} \cdot 5700}{1,00} = 354 + 773 = 1127 \text{ kN}$$

where

 $A_{\rm nt}$ is net area subjected to tension

$$A_{\rm nt} = 2 \cdot t_{\rm p} \cdot (l_{\rm nt}) = 2 \cdot 15 \cdot (50 - 9) = 1230 \,{\rm mm}^2$$

 A_{nv} is net area subjected to shear

$$A_{\rm nv} = 2 \cdot t_{\rm p} \cdot (l_{\rm nv}) = 2 \cdot 15 \cdot (45 + 95 + 95 - 18 - 18 - 9) = 5700 \,{\rm mm}^2$$

Reliability condition:

$$\frac{F_{\rm Ed}}{V_{\rm eff,2, Rd}} = \frac{150}{1127} = 0.13 \le 1.0 \qquad => condition is satisfied$$

Fillet weld

 $F_{\rm Ed} = 150 \, \rm kN$ action of secondary beam

a = 4 mmeffective throat thickness of a fillet weldL = 272 mmeffective length of a fillet weld

$$\tau_{\rm II} = \frac{F_{\rm Ed}}{2 \cdot L \cdot a} = \frac{150.10^3}{2 \cdot 272 \cdot 4} = 69 \text{ MPa}$$

 $\sigma_{\!\scriptscriptstyle \perp} = \tau_{\!\scriptscriptstyle \perp} = 0 \ \mathrm{MPa}$



Reliability conditions:

$$\sqrt{\sigma_{\perp}^{2} + 3 \cdot \left(\tau_{\perp}^{2} + \tau_{\Pi}^{2}\right)} \leq \frac{f_{u}}{\beta_{w} \cdot \gamma_{M2}}$$

$$\sqrt{0^{2} + 3 \cdot \left(0^{2} + 69^{2}\right)} \leq \frac{360}{0.8 \cdot 1.25}$$

$$120 \text{ MPa} \leq 360 \text{ MPa} \qquad => \text{ condition is satisfied}$$

$$\sigma_{\perp} \leq \frac{0.9 \cdot f_{u}}{\gamma_{M2}}$$

 $0 \text{ MPa} \le \frac{0.9 \cdot 360}{1.25} = 259 \text{ MPa} \implies \text{condition is satisfied}$